

**SOLVING EQUATIONS OF ONE VARIABLE ALGEBRAICALLY**

**ALGEBRA** uses the concept of isolating the variable by **applying the inverse ("Opposite")** to **BOTH** sides of the Equation

- if you can solve the "one step" problem scenarios below (a-f). You can solve any multi-step Equation.

a)  $x + 7 = -9$     b)  $7x = -21$     c)  $\frac{x}{-7} = -4$     d)  $-x = 5$

$$\begin{array}{r} x + 7 = -9 \\ -7 \quad -7 \\ \hline x = -16 \end{array}$$

$$\begin{array}{r} 7x = -21 \\ \frac{7x}{7} = \frac{-21}{7} \\ \hline x = -3 \end{array}$$

$$\begin{array}{r} (-7)x = -4(-7) \\ \frac{(-7)x}{-7} = \frac{-4(-7)}{-7} \\ \hline x = 28 \end{array}$$

$$\begin{array}{r} -x = 5 \\ \frac{-x}{-1} = \frac{5}{-1} \\ \hline x = -5 \end{array}$$

e)  $\frac{2}{3}x = 12$     f)  $-\frac{2}{3}x = \frac{4}{5}$

$$\begin{array}{r} \frac{3}{2} \cdot \frac{2}{3}x = 12 \cdot \frac{3}{2} \\ \hline x = \frac{36}{2} \\ \hline x = 18 \end{array}$$

$$\begin{array}{r} (-\frac{3}{2}) \cdot (-\frac{2}{3})x = \frac{4}{5} \cdot (-\frac{3}{2}) \\ \hline x = -\frac{12}{5} \\ \hline x = -\frac{6}{5} \end{array}$$



"Examples e & f are solved multiplying by the **RECIPROCAL** of the fraction next to the variable. If the fraction is (-), then it's reciprocal is also (-). You could solve Ex.'s b through d, similarly."

**MULTI-STEP PROBLEMS**

g)  $3k - 5 = -21$     h)  $\frac{r-5}{3} = -21$     i)  $\frac{p}{3} - 5 = -21$

$$\begin{array}{r} 3k - 5 = -21 \\ +5 \quad +5 \\ \hline 3k = -16 \\ \frac{3k}{3} = \frac{-16}{3} \\ \hline k = -\frac{16}{3} \end{array}$$

$$\begin{array}{r} (3) \frac{r-5}{3} = -21(3) \\ \hline r-5 = -63 \\ +5 \quad +5 \\ \hline r = -58 \end{array}$$

$$\begin{array}{r} \frac{p}{3} - 5 = -21 \\ +5 \quad +5 \\ \hline \frac{p}{3} = -16 \\ (3) \frac{p}{3} = -16(3) \\ \hline p = -48 \end{array}$$

"Notice the **DIFFERENCE** between Example h) and i)."

j)  $8 = 4(3c + 5)$

$$\begin{array}{r} 8 = 4(3c + 5) \\ \text{Mult.} \\ 8 = 12c + 20 \\ -20 \quad -20 \\ \hline -12 = 12c \\ \frac{-12}{12} \quad \frac{12c}{12} \\ \hline -1 = c \end{array}$$

$-1 = c$  or  $c = -1$

k)  $-\frac{1}{2}(x-6) = 4$

$$\begin{array}{r} (-\frac{2}{1}) \cdot (-\frac{1}{2})(x-6) = 4(-\frac{2}{1}) \\ \hline (x-6) = -4 \\ +6 \quad +6 \\ \hline x = -2 \end{array}$$

**FINALLY: MAKE SURE TO "KYSS" your work. KEEP YOUR STEPS STRAIGHT**

- Always re-copy original Problem. Never ruin it in your work.
- Use the line paper to guide you per step. Each step is a Math full sentence, compared to your writing class.